

 **Announcements**

PRACTICE	LABS	TESTS
Practice problems (1-14,16)	<ul style="list-style-type: none"> <li>Exploding carts interactive</li> <li>Collisions Interactive</li> <li>Roller Coaster Lab</li> </ul>	Unit 11 Test Thursday 2/28

**Elastic Collisions**

LEARNING TARGET	DESCRIPTION
11.2	I can define, interpret, and solve problems involving the Law of Conservation of Momentum.
11.3	I can define, analyze, and solve problems involving two particle collision.

**Review Momentum and Impulse**

Momentum

$$\mathbf{p} = m \mathbf{v}$$

Impulse-Momentum Theorem

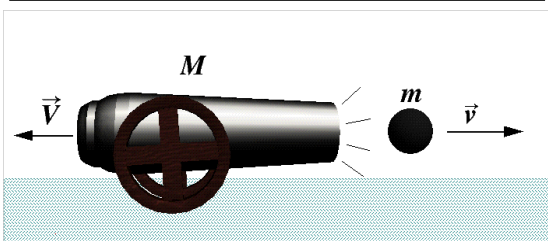
$$F \Delta t = \Delta p = p_f - p_i$$

**Conservation of Momentum**

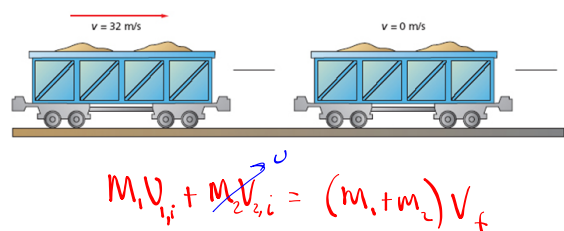
If the net external force acting on an object, or system, is zero, its momentum is conserved.

$$\vec{p}_i = \vec{p}_f$$

**Conservation of Momentum**

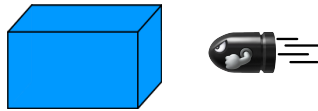


**Inelastic Collisions in One Dimension**



### Through and Through

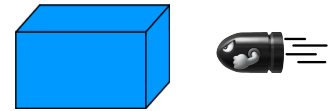
Bullet Bill has a mass of 350.0 g and is traveling toward a block of ballistics gel at 900 mph. Bill travels all the way through the 5.0 kg block of gel, and exits going half his original speed. How fast is the ballistics gel traveling after the collision?



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OBJECTS	MOMENTUM BEFORE (kg·m/s)	MOMENTUM AFTER (kg·m/s)
BILL		
GEL		
TOTAL		

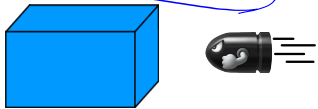


### Through and Through

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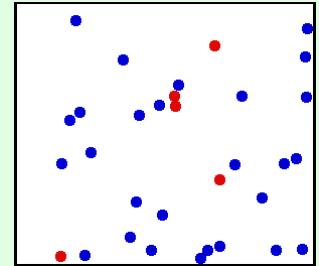
OBJECTS	MOMENTUM BEFORE (kg·m/s)	MOMENTUM AFTER (kg·m/s)
BILL	$(0.350 \text{ kg})(402 \text{ m/s}) = 141 \text{ kg·m/s}$	$(0.350 \text{ kg})(201 \text{ m/s}) = 70 \text{ kg·m/s}$
GEL	$(5.0 \text{ kg})(0 \text{ m/s}) = 0 \text{ kg·m/s}$	$(5.0 \text{ kg})(v_f)$
TOTAL	141 kg·m/s	141 kg·m/s

$70 \text{ kg} + (5 \text{ kg})V_f = 141$   
 $V_f = 14 \text{ m/s}$

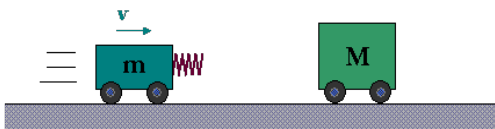


### 2 Types of Collisions

**Elastic collisions** are when objects bounce, and do not stick together on impact.

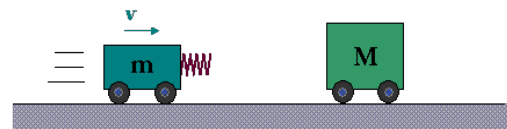


### Elastic Collisions



- [Physicsclassroom.com](http://Physicsclassroom.com)
- Interactives
- Momentum and Collisions
- Collision Carts

### Elastic Collisions



One cart (mass = m) moves with a velocity v and collides elastically with another cart (mass = M) that is stationary. What is the result of the collisions in the following situations:

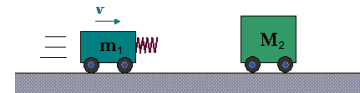
1.  $m = M$
2.  $m > M$
3.  $m < M$

### Elastic Collisions



4. One cart ( $m_1 = 1.50 \text{ kg}$ ) moves with a velocity  $v = 5.30 \text{ m/s}$  and collides elastically with another cart ( $M_2 = 5.00 \text{ kg}$ ) that is stationary. The collision is completely elastic and cart  $M_2$  has a speed of  $2.45 \text{ m/s}$  after the collision. What is the speed and direction of cart  $m_1$  after the collision?
- What is the speed and direction of cart  $m_1$  after the collision?
  - What is the change in kinetic energy after the collision?

### Elastic Collisions



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OBJECTS	MOMENTUM BEFORE (kg·m/s)	MOMENTUM AFTER (kg·m/s)
$m_1$	$(1.50 \text{ kg})(5.30 \text{ m/s}) = 7.95 \text{ kg}\cdot\text{m/s}$	$(1.50 \text{ kg})(v_{1,f})$
$M_2$	$(5.0 \text{ kg})(0 \text{ m/s}) = 0 \text{ kg}\cdot\text{m/s}$	$(5.0 \text{ kg})(2.45 \text{ m/s}) = 12.25 \text{ kg}\cdot\text{m/s}$
<b>TOTAL</b>	<b>7.95 kg·m/s</b>	<b>7.95 kg·m/s</b>

$$(1.50 \text{ kg})(v_{1,f}) + 12.25 \text{ kg}\cdot\text{m/s} = 7.95 \text{ kg}\cdot\text{m/s}$$

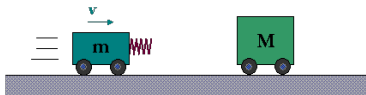
$$(1.50 \text{ kg})(v_{1,f}) = -4.30 \text{ kg}\cdot\text{m/s}$$

$$v_{1,f} = -2.90 \text{ m/s}$$

$$K_i = \frac{1}{2} (1.50 \text{ kg})(5.30)^2 = 21.1 \text{ J}$$

$$K_f = \frac{1}{2} (1.5 \text{ kg})(2.90)^2 + \frac{1}{2} (5 \text{ kg})(2.45)^2 = 21.3 \text{ J}$$

### Elastic Collisions



Momentum

$$m_1 v_1 + m_2 v_2 = m_1 v_{1,f} + m_2 v_{2,f}$$

Kinetic Energy

$$\frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2 = \frac{1}{2} m_1 v_{1,f}^2 + \frac{1}{2} m_2 v_{2,f}^2$$

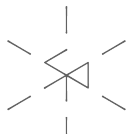
### Elastic Collisions In One Dimension

Initial Conditions

$$v_{1,i} = v_0 \text{ and } v_{2,i} = 0$$

$$v_{1,f} = \left( \frac{m_1 - m_2}{m_1 + m_2} \right) v_0$$

$$v_{2,f} = \left( \frac{2m_1}{m_1 + m_2} \right) v_0$$

Science  Practice

**PROBLEMS**

**(17-19)**