



PRACTICE	LABS	TESTS
Unit 12 Problems (1-12)	Roller Coaster Lab Corrections	Unit 12 Test Tuesday (4/4/19)

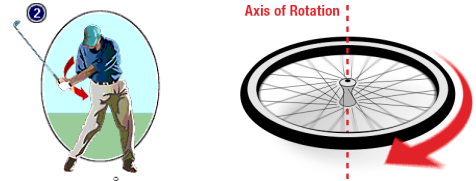
Prom Royalty [bit.ly/bshprom19](http://bit.ly/bshprom19)

## Rolling Motion and the Moment of Inertia

Learning Target

12.2

I can describe, interpret, and solve problems involving rolling motion and the moment of inertia.



### Moment Of Inertia

The resistance to rotation is called the moment of inertia.

I

PULL

Units

kg · m<sup>2</sup>

## UNIT 12 REVIEW

### Key Concepts

- The moment of inertia of an object depends on the way the object's mass is distributed about the rotational axis. For a point object:

$I = mr^2$

Hoop or cylindrical shell $I = MR^2$	Disk or solid cylinder $I = \frac{1}{2} MR^2$	Disk or solid cylinder (axis at rim) $I = \frac{3}{2} MR^2$	Long thin rod (axis through midpoint) $I = \frac{1}{12} ML^2$	Long thin rod (axis at one end) $I = \frac{1}{3} ML^2$
Hollow sphere $I = \frac{2}{3} MR^2$	Solid sphere $I = \frac{2}{5} MR^2$	Solid sphere (axis through center) $I = \frac{2}{5} MR^2$	Solid plate (axis through center, in plane of plate) $I = \frac{1}{12} ML^2 + W^2$	Solid plate (axis perpendicular to plane of plate) $I = \frac{1}{12} ML^2 + W^2$

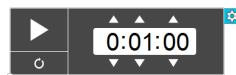
### UNIT 12 IN CLASS PROBLEMS



Retrieval Practice [Practice Testing]

You learned that an object's motion can be described using big picture concepts of kinetic energy and momentum.

12. In one minute, write down at least 3 things that you remember about kinetic energy and at least 3 things you remember about momentum.



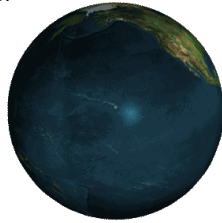
<p style="text-align: center;"><u>KE</u></p> <p style="text-align: center;">mass in motion</p> <div style="border: 1px solid blue; padding: 5px; display: inline-block;"> <math display="block">K = \frac{1}{2}mv^2</math> </div> <p style="text-align: center;"><math>K + u = E</math></p> <p style="text-align: center;">Scalar</p> <p style="text-align: center;">J</p> <p style="text-align: center;">Mass <math>\rightarrow</math> Dir. Prop.</p> <p style="text-align: center;"><math>\vec{V} \rightarrow</math> Dir. Quad.</p>	<p style="text-align: center;"><u>Momentum</u></p> <p style="text-align: center;">mass in motion</p> <div style="border: 1px solid blue; padding: 5px; display: inline-block;"> <math display="block">\vec{p} = m\vec{v}</math> </div> <p style="text-align: center;">Vector</p> <p style="text-align: center;"><math>kg \cdot \frac{m}{s}</math></p> <p style="text-align: center;">Dir. Prop.</p>
---	---

## Rotational Kinetic Energy

The rotational kinetic energy of an object is one-half the product of its moment of inertia and the square of its angular speed.

$$K = \frac{1}{2}mv^2$$

$$K = \frac{1}{2}I\omega^2$$



## Rotational Kinetic Energy

Vector of Scalar?

$$K = \frac{1}{2}I\omega^2$$

Units?  $kg \cdot m^2 \left(\frac{rad}{s}\right)^2 = J$

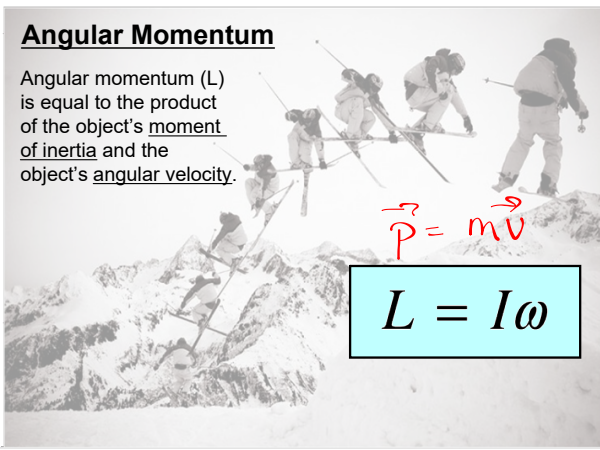
Relationship?

$I \rightarrow$  Direct, Prop.  $I = mr^2$

$\omega \rightarrow$  Direct, Quad.

## Angular Momentum

Angular momentum (L) is equal to the product of the object's moment of inertia and the object's angular velocity.



$$\vec{p} = m\vec{v}$$

$$L = I\omega$$

## Angular Momentum

Vector of Scalar?

$$L = I\omega$$

Units?  $kg \cdot m^2 \left(\frac{rad}{s}\right) = \frac{kg \cdot m^2}{s}$

Relationship?

Direct, Prop.

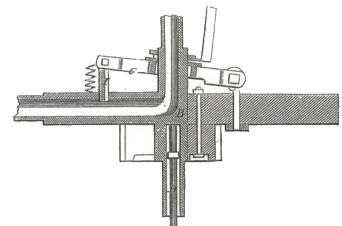
## Confederate Steam Gun



On April 19, 1861 there was a clash between secessionists and Federal troops in Baltimore, Maryland. Readers of newspapers across the United States learned of a strange, and allegedly powerful steam powered weapon brought forth to fend off more Union troops seeking to pass through the town by rail to Washington.

## Confederate Steam Gun

A steam engine powered a rotary wheel that flung ball ammunition in a closed circle before releasing it at high speeds from a barrel that could pivot within a large metal shield protecting the crew. The entire device was heavy, requiring a large boiler in addition to the barrel, rotary, and shield, and typically had to be moved with horses. A member of the crew needed to keep feeding ammunition into the weapon as it tore through rounds.



### Confederate Steam Gun

The rotating barrel had a mass of 5.0 kg and rotated with a radius of 1.5 m. The barrel rotated at 400 rpm and it can be assumed to be a long thin rod rotating at one end. Calculate the following values:

- a) the moment of inertia for the barrel.

$$I = \frac{1}{3} mL^2 = \frac{1}{3} (5 \text{ kg})(1.5 \text{ m})^2 = 3.75 \text{ kg}\cdot\text{m}^2$$

- b) the kinetic energy of the barrel.

$$K = \frac{1}{2} I \omega^2 = \frac{1}{2} (3.75 \text{ kg}\cdot\text{m}^2) \left(41.9 \frac{\text{rad}}{\text{s}}\right)^2 = 3300 \text{ J}$$

- c) the angular momentum of the barrel.

$$L = I \omega$$

$$L = (3.75 \text{ kg}\cdot\text{m}^2) \left(41.9 \frac{\text{rad}}{\text{s}}\right)$$

$\omega = 400 \frac{\text{rev}}{\text{min}} \times \frac{2\pi \text{ rad}}{1 \text{ rev}} \times \frac{1 \text{ min}}{60 \text{ s}}$

$$L = 160 \frac{\text{kg}\cdot\text{m}^2}{\text{s}}$$

