



**Announcements**

PRACTICE	LABS	TESTS
Unit 12 Problems (1-17)	Balancing Lab (Due Tues. 3/19)	Unit 12 Test Tuesday (3/26/19)

## TORQUE

**12.3** I can define, analyze, and solve problems involving torque.





## UNIT 12 REVIEW

**Key Concepts**

- Angular position and its changes are measured in radians. One complete revolution is  $2\pi$  rad.
- Angular velocity is given by the following equation.

$$\omega = \frac{\Delta\theta}{\Delta t}$$

- Angular acceleration is given by the following equation.

$$\alpha = \frac{\Delta\omega}{\Delta t}$$

- For a rotating, rigid object, the angular displacement, velocity, and acceleration can be related to the linear displacement, velocity, and acceleration for any point on the object.

$$d = r\theta \quad v = r\omega \quad a = r\alpha$$

**Rotational Kinetic Energy and Angular Momentum**

The rotational kinetic energy of an object is one-half the product of its moment of inertia and the square of its angular speed.

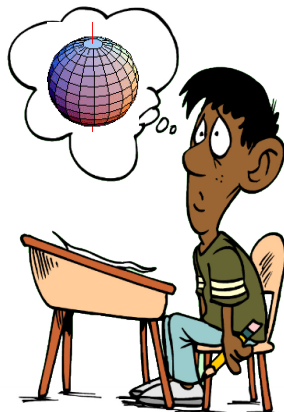
$$K = \frac{1}{2} I \omega^2$$

Angular momentum (L) is equal to the product of the object's moment of inertia and the object's angular velocity.

$$L = I \omega$$


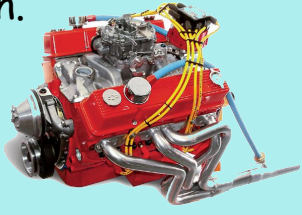
## Question

How do you get an object to rotate?

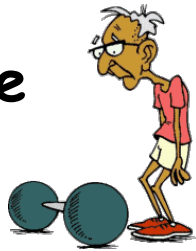


## Torque

**Torque** ( $\tau$ ) is a measure of how effectively a force causes rotation.

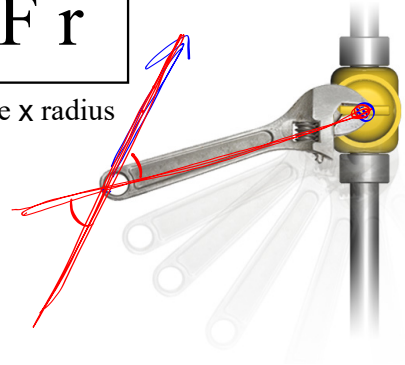
# The Torque Experience



## Definition of Torque (tangential force)

$$\tau = F r$$

torque = force x radius



## Torque

Vector of Scalar?

$$\tau = F r$$

Units?  $N \cdot m$

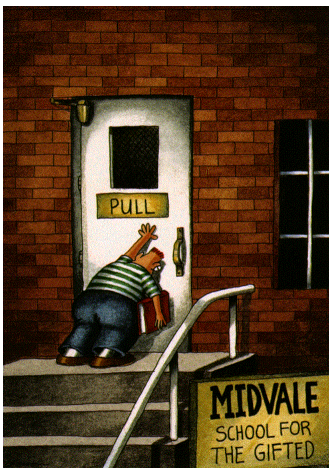
Relationship?

Direct Prop.

## Sign of Torque

$\tau > 0$  if the torque causes a counterclockwise angular acceleration

$\tau < 0$  if the torque causes a clockwise angular acceleration

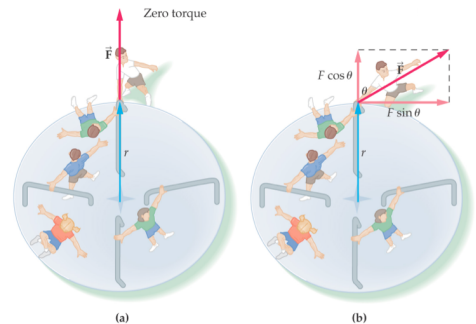


Physics Opens Doors!



## Torque

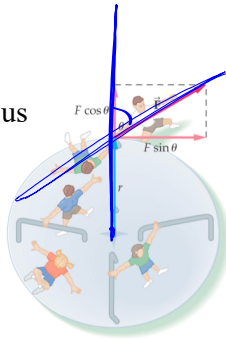
Only the tangential component of force cause a torque.



**Definition of Torque (nontangential force)**

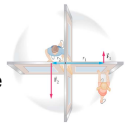
$$\tau = (F \sin \theta) r$$

torque = (force x sin  $\theta$ ) x radius

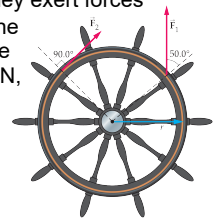


**UNIT 12 IN CLASS PROBLEMS**

15. To open a revolving door a tangential force  $F$  if applied at a distance  $r$  from the axis of rotation. If the minimum torque required to open the door is 3.1 N·m, what force must be applied if  $r$  if (a) 0.94 m or (b) 0.35 m?



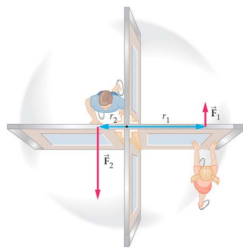
16. Captains Sparrow and Barbosa are in a disagreement about which way to turn the ship. They exert forces shown below on the ship's wheel. The wheel has a radius of 0.74 m, and the two forces have magnitudes  $F_1 = 72$  N, and  $F_2 = 58$  N. (a) Find the torque caused by  $F_1$ . (b) Find the torque caused by  $F_2$ . (c) In which direction does the wheel turn as a result of these two forces?



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$$\tau = (F \sin \theta) r$$

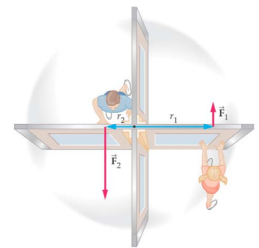


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$$(a) F_1 = \frac{\tau}{r_1} = 3.3 \text{ N}$$

$$(b) F_2 = \frac{\tau}{r_2} = 8.9 \text{ N}$$



**UNIT 12 IN CLASS PROBLEMS**

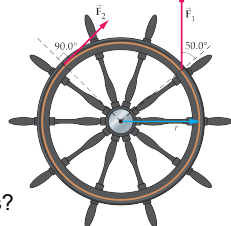
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(a) Find the torque caused by  $F_1$ .

$$\tau_1 = (F_1 \sin \theta) r_1$$

(b) Find the torque caused by  $F_2$ .

(c) In which direction does the wheel turn as a result of these two forces?



**UNIT 12 IN CLASS PROBLEMS**

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(a) Find the torque caused by  $F_1$ .

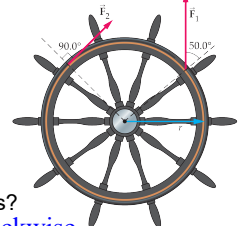
$$\tau_1 = (72 \text{ N} \sin 50.0^\circ) r = 41 \text{ N}\cdot\text{m}$$

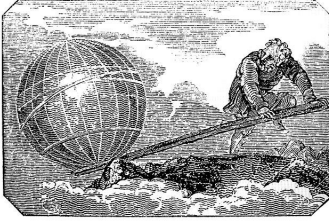
(b) Find the torque caused by  $F_2$ .

$$\tau_2 = -(58 \text{ N} \sin 90.0^\circ) r = -43 \text{ N}\cdot\text{m}$$

(c) In which direction does the wheel turn as a result of these two forces?

$$\tau_{\text{total}} = \tau_1 + \tau_2 = -2 \text{ N}\cdot\text{m} \quad \text{Clockwise}$$





Archimedes is said to have remarked about the lever: "Give me a place to stand on, and I will move the Earth."

# UNIT 12 PROBLEMS

## (18-23)