

# Announcements

PRACTICE	LABS	TESTS
Unit 12 Problems (1-23)	Balancing Lab Corrections by Friday	Unit 12 Test Tuesday (3/26/19)

## Angular Momentum



12.3

I can define, analyze, and solve problems involving torque.

## TORQUE SUMMARY

Torque due to a tangential force:  $\tau = rF$

Torque in general:  $\tau = rF \sin \theta$

Newton's second law for rotation:  $\tau = I\alpha$

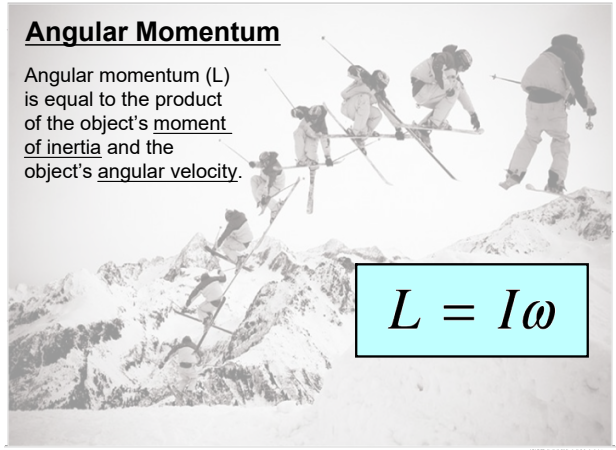
Kinetic energy of rotation:  $K = \frac{1}{2}I\omega^2$

Moment of inertia:  $I = \sum m_i r_i^2$

Angular momentum:  $L = I\omega$

### Angular Momentum

Angular momentum ( $L$ ) is equal to the product of the object's moment of inertia and the object's angular velocity.



$$L = I\omega$$

## Angular Impulse

$$\text{Angular Impulse} = \Delta L$$

### Angular Impulse - Angular Momentum Theorem

$$\tau \Delta t = \Delta L$$

Define the conservation of momentum and give three real world applications.

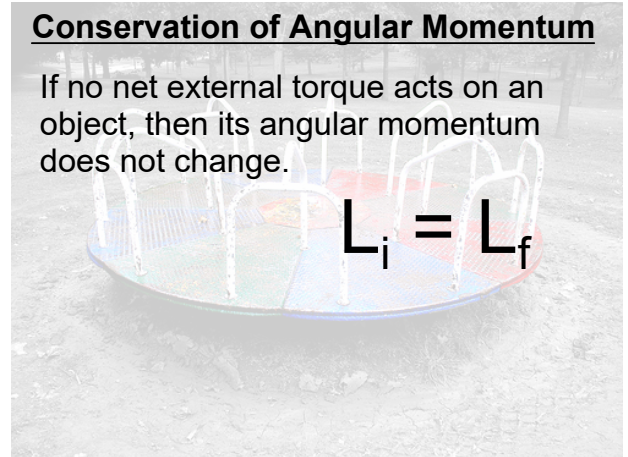


Retrieval Practice  
[Practice Testing]

**Conservation of Angular Momentum**

If no net external torque acts on an object, then its angular momentum does not change.

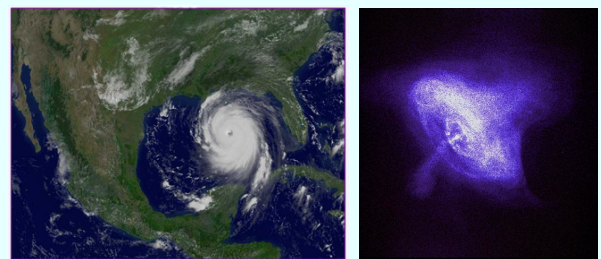
$$L_i = L_f$$



**Changing M.O.I.**



**Applications of the Law of Conservation of Momentum**



**Applications of the Law of Conservation of Momentum**

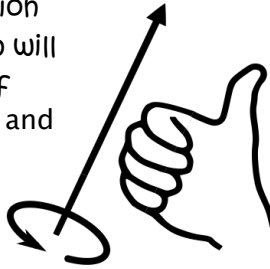


**Helicopters**



## The Right-Hand Rule

Curl the fingers of the right hand in the direction of rotation. The thumb will point in the direction of the angular velocity,  $\vec{\omega}$ , and angular momentum,  $\vec{L}$ .



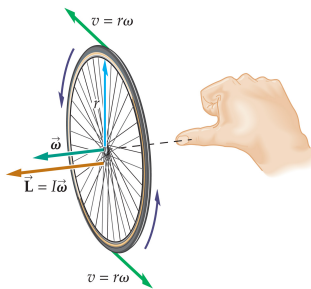
## The Vector Nature of Angular Velocity and Momentum

When an object rotates it is said to have an angular velocity,  $\vec{\omega}$ , and therefore angular momentum,  $\vec{L}$ . How do we determine the direction of these two vector quantities?

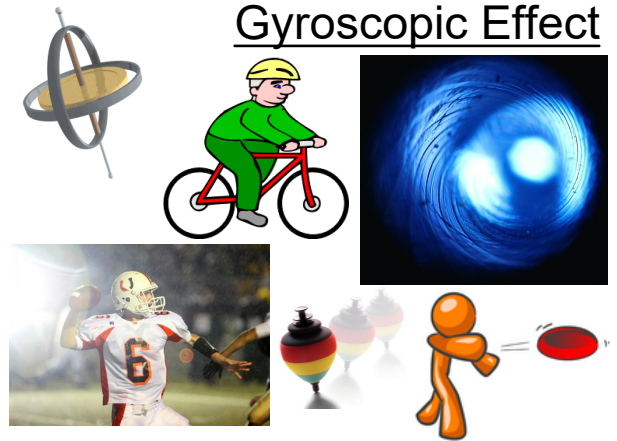


## Angular Momentum

$$\vec{L} = I \vec{\omega}$$



## Gyroscopic Effect

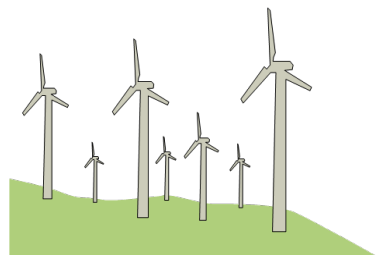


### UNIT 12 IN CLASS PROBLEMS

- In a light wind, a windmill experiences a constant torque of 255 N·m. If the windmill is initially at rest, what is its angular momentum 2.00 s later?
- Initially holding her arms outstretched, a figure starts to spin with an angular speed of 3.7 rad/s. Her moment of inertia in this case is 5.33 kg·m<sup>2</sup>. While still spinning, the figure skater pulls her arms in to her chest, reducing the moment of inertia to 1.60 kg·m<sup>2</sup>. What is the figure skater's angular speed now?

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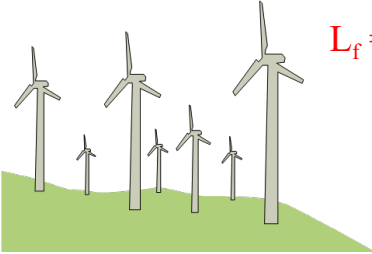


**UNIT 12 IN CLASS PROBLEMS**

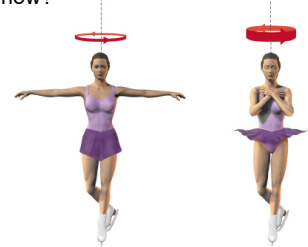
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$$L_f = \tau \Delta t$$

$$L_f = 510 \text{ kg}\cdot\text{m}^2$$

**UNIT 12 IN CLASS PROBLEMS**

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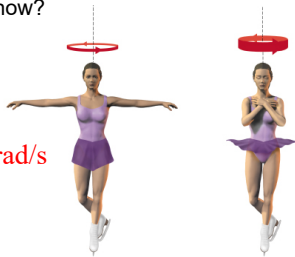
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$$L_i = L_f$$

$$I_i \omega_i = I_f \omega_f$$

$$\omega_f = \left( \frac{I_i}{I_f} \right) \omega_i = 12.5 \text{ rad/s}$$

**UNIT 12 PROBLEMS****(1-23)**